

January 2007  
6684 Statistics S2  
Mark Scheme

Question Number	Scheme	Marks
<p>1. (a)</p> <p>(b) (i)</p> <p>(ii)</p>	<p>A random variable; function of known observations (from a population). data OK</p> <p>Yes</p> <p>No</p>	<p><b>B1</b> <b>B1</b> <b>(2)</b></p> <p><b>B1</b> <b>(1)</b></p> <p><b>B1</b> <b>(1)</b></p> <p><b>Total 4</b></p>
<p>2. (a)</p> <p>(b)</p>	<p><math>P(J \geq 10) = 1 - P(J \leq 9)</math>                      or <math>= 1 - P(J &lt; 10)</math></p> <p><math>= 1 - 0.9919</math>    implies method</p> <p><math>= 0.0081</math>    awrt 0.0081</p> <p><math>P(K \leq 1) = P(K = 0) + P(K = 1)</math> both, implied below even with '25' missing</p> <p><math>= (0.73)^{25} + 25(0.73)^{24}(0.27)</math>                      clear attempt at '25' required</p> <p><math>= 0.00392</math>    awrt 0.0039 implies M</p>	<p><b>M1</b></p> <p><b>A1</b> <b>(2)</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b> <b>(3)</b></p> <p><b>Total 5</b></p>



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4.		
(a)	$\lambda > 10$ or large <span style="float: right;"><math>\mu</math> ok</span>	<b>B1</b> <b>(1)</b>
(b)	The Poisson is discrete and the normal is continuous.	<b>B1</b> <b>(1)</b>
(c)	Let $Y$ represent the number of yachts hired in winter $P(Y < 3) = P(Y \leq 2)$ <span style="float: right;"><math>P(Y \leq 2)</math> &amp; Po(5)</span>  $= 0.1247$ <span style="float: right;">awrt 0.125</span>	<b>M1</b>  <b>A1</b> <b>(2)</b>
(d)	Let $X$ represent the number of yachts hired in summer $X \sim \text{Po}(25)$ . $N(25, 25)$ all correct, can be implied by standardisation below $P(X > 30) \approx P\left(Z > \frac{30.5 - 25}{5}\right)$ <span style="float: right;"><math>\pm</math> standardise with 25 &amp; 5; <math>\pm 0.5</math> c.c.</span>  $\approx P(Z > 1.1)$ <span style="float: right;">1.1</span>  $\approx 1 - 0.8643$ <span style="float: right;">‘one minus’</span>  $\approx 0.1357$ <span style="float: right;">awrt 0.136</span>	<b>B1</b> <b>M1;M1</b> <b>A1</b> <b>M1</b> <b>A1</b> <b>(6)</b>
(e)	no. of weeks $= 0.1357 \times 16$ <span style="float: right;">ANS (d)x16</span>  $= 2.17$ or 2 or 3 <span style="float: right;">ans&gt;16 M0A0</span>	<b>M1</b>  <b>A1</b> <b>(2)</b> <b>Total 12</b>

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5.		
(a)	$f(x) = \begin{cases} \frac{1}{\beta - \alpha}, & \alpha < x < \beta, \\ 0, & \text{otherwise.} \end{cases}$	<p>function including inequality, 0 otherwise</p> <p><b>B1,B1</b></p> <p><b>(2)</b></p>
(b)	$\frac{\alpha + \beta}{2} = 2, \quad \frac{3 - \alpha}{\beta - \alpha} = \frac{5}{8}$ $\alpha + \beta = 4$ $3\alpha + 5\beta = 24$ $3(4 - \beta) + 5\beta = 24$ $2\beta = 12$ $\beta = 6$ $\alpha = -2$	<p>or equivalent</p> <p><b>B1,B1</b></p> <p>attempt to solve 2 eqns</p> <p><b>M1</b></p> <p>both</p> <p><b>A1</b></p> <p><b>(4)</b></p>
(c)	$E(X) = \frac{150 + 0}{2} = 75 \text{ cm}$	<p>75</p> <p><b>B1</b></p> <p><b>(1)</b></p>
(d)	$\text{Standard deviation} = \sqrt{\frac{1}{12}(150 - 0)^2}$ $= 43.30127\dots \text{cm}$	<p><b>M1</b></p> <p><math>25\sqrt{3}</math> or awrt 43.3</p> <p><b>A1</b></p> <p><b>(2)</b></p>
(e)	$P(X < 30) + P(X > 120) = \frac{30}{150} + \frac{30}{150}$ $= \frac{60}{150} \text{ or } \frac{2}{5} \text{ or } 0.4 \text{ or equivalent fraction}$	<p>1st or at least one fraction, + or double</p> <p><b>M1,M1</b></p> <p><b>A1</b></p> <p><b>(3)</b></p> <p><b>Total 12</b></p>



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7. (a)	$1 - F(0.3) = 1 - (2 \times 0.3^2 - 0.3^3)$ $= 0.847$	'one minus' required  <b>M1</b> <b>A1</b> <b>(2)</b>
(b)	$F(0.60) = 0.5040$ $F(0.59) = 0.4908$ <p>0.5 lies between therefore median value lies between 0.59 and 0.60.</p>	both required awrt 0.5, 0.49  <b>M1A1</b>  <b>B1</b> <b>(3)</b>
(c)	$f(x) = \begin{cases} -3x^2 + 4x, & 0 \leq x \leq 1, \\ 0, & \text{otherwise.} \end{cases}$	attempt to differentiate, all correct  <b>M1A1</b> <b>(2)</b>
(d)	$\int_0^1 xf(x)dx = \int_0^1 -3x^3 + 4x^2 dx$ $= \left[ \frac{-3x^4}{4} + \frac{4x^3}{3} \right]_0^1$ $= \frac{7}{12} \text{ or } 0.58\dot{3} \text{ or } 0.583 \text{ or equivalent fraction}$	attempt to integrate $xf(x)$  sub in limits  <b>M1</b>  <b>M1</b>  <b>A1</b> <b>(3)</b>
(e)	$\frac{df(x)}{dx} = -6x + 4 = 0$ $x = \frac{2}{3} \text{ or } 0.\dot{6} \text{ or } 0.667$	attempt to differentiate $f(x)$ and equate to 0  <b>M1</b>  <b>A1</b> <b>(2)</b>
(f)	mean < median < mode, therefore negative skew.	Any pair, cao  <b>B1,B1</b> <b>(2)</b>  <b>Total 14</b>